

Chapter 1- Measurement

Measurements } Science & Engineering, So, how things are measured and compared.
 Comparisons } based on \Rightarrow experiments to establish the units for those measurements and comparisons.

measure the quantities: such as length, time, mass, temperature, pressure, electric current

in their own units (by comparison with a standard)

i.e. meter (m) for the quantity length. • standard corresponds to exactly 1.0 units of the quantity
 • standard for the length (1.0 m)
 \Rightarrow distance traveled by light in a vacuum during a certain fraction of a second.

So many physical quantities !! { not all independent } speed $\sim \frac{\text{length}}{\text{time}}$ } Becomes small number of physical quantities.

Units for three SI Base Quantities

| Quantity | Unit Name | Unit Symbol |
|----------|-----------|-------------|
| length | meter | m |
| Time | second | s |
| Mass | kilogram | kg |

[L] [M] [T] Base quantities Base standards (Seven)

Derived Units:

Units are defined in terms of base units.

i.e. SI unit for power, Watt
 $1 \text{ Watt} = 1 \text{ W} = 1 \text{ kg} \frac{\text{m}^2}{\text{s}^3}$

SI Units \equiv metric system

Example: Find the distance that light travels in one year.

$c = 2.998 \times 10^8 \text{ m/s}$ light year, ly

Base Unit: time $1 = \frac{60 \text{ sec}}{1 \text{ min}}$, $1 = \frac{365.25 \text{ day}}{1 \text{ year}}$, $1 \text{ ly} = \frac{(2.998 \times 10^8 \text{ m/s})}{(\text{year})}$

$$1 \text{ ly} = (2.998 \times 10^8 \text{ m/s}) \left(\frac{365.25 \text{ day}}{1 \text{ year}} \right) \left(\frac{24 \text{ hours}}{1 \text{ day}} \right) \left(\frac{60 \text{ min}}{1 \text{ hour}} \right) \left(\frac{60 \text{ sec}}{1 \text{ min}} \right)$$

$$= 9.461 \times 10^{15} \text{ m}$$

Very large quantities; we need scientific notation \Rightarrow powers of 10
 Very small quantities; we need scientific notation \Rightarrow powers of 10

$0.00035 \xrightarrow{2 \sim \# \text{ of significant figures}} 3.5 \times 10^{-4}$ or 3.5E^{-4} ; exponent of ten
 $0.000325400 \xrightarrow{6} 3.25400 \times 10^{-4}$
 $2500 \xrightarrow{2} 2.5 \times 10^3$
 $3560000000 \xrightarrow{3} 3.56 \times 10^9$

10 sf? Do we know the quantity so accurate? Solution is the scientific notation.

See Table 1.2 for Prefixes for SI Units.

1.27×10^9 watts = 1.27 gigawatts = 1.27 GW
 2.35×10^{-9} s = 2.35 nanosecond = 2.35 ns

See lecture notes for "Changing Units", Chain-link conversion

Example: Uncertainty, How accurate?

Page width? a measure: 1 mm divisions (accuracy)

21.6 cm \pm 0.1 cm plus minus 0.1: Error in measurement

Percentage error in measurement: $(\frac{0.1}{21.6}) \times 100 = 0.5\%$

Page area?

21.6 cm (\pm 0.1)
 27.9 cm (\pm 0.1)

(0.4%) what is the percentage error in measurement?

$(21.6 \text{ cm}) \times (27.6 \text{ cm}) = 603 \text{ cm}^2$
 what about uncertainty in measurement of area?

(0.4 + 0.5) addition 0.9 \rightarrow 0.9%
 $(0.9) \times (603 \text{ cm}^2) = 5 \text{ cm}^2 \Rightarrow 603 \pm 5 \text{ cm}^2$

Example: Significant figures (sf) Physical properties \rightarrow uncertainty

2.00 m (3 sf) \leftarrow OR 1.995 m ?
 2.000 m (4 sf) \leftarrow 2.005 m

603 cm² (3 sf) \leftarrow 602.5 cm²
 603.5 cm²

0.00035 (2 sf, not 6 sf)

mass of earth 5.98×10^{24} kg (3 sf)
 6.0×10^{24} kg (2 sf)

In calculations, in exams!
 $\frac{3.0}{11.0} = 0.27272727 \dots$ with calculator

\Rightarrow least number of sf!
 $\Rightarrow 0.27 \checkmark$