Ceng 272 - Quiz 3

Solve all questions.

For Monday section

1. One prominent physician claims that 70% of those with lung cancer are chain smokers. If his assertion is correct, find the probability that of 10 such patients recently admitted to a hospital, fewer than half are chain smokers. (See Table)

- 2. If 7 cards are dealt from an ordinary deck of 52 playing cards, what is the probability that
 - (a) exactly 2 of them will be face cards?
 - (b) at least 1 of them will be a queen?

For Thursday section

1. One prominent physician claims that 70% of those with lung cancer are chain smokers. If his assertion is correct, find the probability that of 20 such patients recently admitted to a hospital, fewer than half are chain smokers. (See Table)

2. To avoid detection at customs, a traveler places 6 narcotic tablets in a bottle containing 9 vitamin pills that are similar in appearance. If the customs official selects 3 of the tablets at random for analysis, what is the probability that the traveler will be arrested for illegal possession of narcotics?

Table A.1 Binomial Probability Table

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Table A.1 (continued) Binomial Probability Sums $\sum_{x=0}^{r} b(x; n, p)$

| _ | | | | | | | 0 | | | | |
|----|----|----------|--------|--------|--------|--------|--------|--------|--------|--------|---------|
| | | <i>p</i> | | | | | | | | | |
| n | r | 0.10 | 0.20 | 0.25 | 0.30 | 0.40 | 0.50 | 0.60 | 0.70 | 0.80 | 0.90 |
| 8 | 0 | 0.4305 | 0.1678 | 0.1001 | 0.0576 | 0.0168 | 0.0039 | 0.0007 | 0.0001 | 0.0000 | |
| | 1 | 0.8131 | 0.5033 | 0.3671 | 0.2553 | 0.1064 | 0.0352 | 0.0085 | 0.0013 | 0.0001 | |
| | 2 | 0.9619 | 0.7969 | 0.6785 | 0.5518 | 0.3154 | 0.1445 | 0.0498 | 0.0113 | 0.0012 | 0.0000 |
| | 3 | 0.9950 | 0.9437 | 0.8862 | 0.8059 | 0.5941 | 0.3633 | 0.1737 | 0.0580 | 0.0104 | 0.0004 |
| | 4 | 0.9996 | 0.9896 | 0.9727 | 0.9420 | 0.8263 | 0.6367 | 0.4059 | 0.1941 | 0.0563 | 0.0050 |
| | 5 | 1.0000 | 0.9988 | 0.9958 | 0.9887 | 0.9502 | 0.8555 | 0.6846 | 0.4482 | 0.2031 | 0.0381 |
| | 6 | | 0.9999 | 0.9996 | 0.9987 | 0.9915 | 0.9648 | 0.8936 | 0.7447 | 0.4967 | 0.1869 |
| | 7 | | 1.0000 | 1.0000 | 0.9999 | 0.9993 | 0.9961 | 0.9832 | 0.9424 | 0.8322 | 0.5695 |
| | 8 | | | | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 9 | 0 | 0.3874 | 0.1342 | 0.0751 | 0.0404 | 0.0101 | 0.0020 | 0.0003 | 0.0000 | | |
| | 1 | 0.7748 | 0.4362 | 0.3003 | 0.1960 | 0.0705 | 0.0195 | 0.0038 | 0.0004 | 0.0000 | |
| | 2 | 0.9470 | 0.7382 | 0.6007 | 0.4628 | 0.2318 | 0.0898 | 0.0250 | 0.0043 | 0.0003 | 0.0000 |
| | 3 | 0.9917 | 0.9144 | 0.8343 | 0.7297 | 0.4826 | 0.2539 | 0.0994 | 0.0253 | 0.0031 | 0.0001 |
| | 4 | 0.9991 | 0.9804 | 0.9511 | 0.9012 | 0.7334 | 0.5000 | 0.2666 | 0.0988 | 0.0196 | 0.0009 |
| | 5 | 0.9999 | 0.9969 | 0.9900 | 0.9747 | 0.9006 | 0.7461 | 0.5174 | 0.2703 | 0.0856 | 0.0083 |
| | 6 | 1.0000 | 0.9997 | 0.9987 | 0.9957 | 0.9750 | 0.9102 | 0.7682 | 0.5372 | 0.2618 | 0.0530 |
| | 7 | | 1.0000 | 0.9999 | 0.9996 | 0.9962 | 0.9805 | 0.9295 | 0.8040 | 0.5638 | 0.2252 |
| | 8 | | | 1.0000 | 1.0000 | 0.9997 | 0.9980 | 0.9899 | 0.9596 | 0.8658 | 0.6126 |
| | 9 | | | | | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 10 | 0 | 0.3487 | 0.1074 | 0.0563 | 0.0282 | 0.0060 | 0.0010 | 0.0001 | 0.0000 | | |
| | 1 | 0.7361 | 0.3758 | 0.2440 | 0.1493 | 0.0464 | 0.0107 | 0.0017 | 0.0001 | 0.0000 | |
| | 2 | 0.9298 | 0.6778 | 0.5256 | 0.3828 | 0.1673 | 0.0547 | 0.0123 | 0.0016 | 0.0001 | |
| | 3 | 0.9872 | 0.8791 | 0.7759 | 0.6496 | 0.3823 | 0.1719 | 0.0548 | 0.0106 | 0.0009 | 0.0000 |
| | 4 | 0.9984 | 0.9672 | 0.9219 | 0.8497 | 0.6331 | 0.3770 | 0.1662 | 0.0473 | 0.0064 | 0.0001 |
| | 5 | 0.9999 | 0.9936 | 0.9803 | 0.9527 | 0.8338 | 0.6230 | 0.3669 | 0.1503 | 0.0328 | 0.0016 |
| | 6 | 1.0000 | 0.9991 | 0.9965 | 0.9894 | 0.9452 | 0.8281 | 0.6177 | 0.3504 | 0.1209 | ,0.0128 |
| | 7 | | 0.9999 | 0.9996 | 0.9984 | 0.9877 | 0.9453 | 0.8327 | 0.6172 | 0.3222 | 0.0702 |
| | 8 | | 1.0000 | 1.0000 | 0.9999 | 0.9983 | 0.9893 | 0.9536 | 0.8507 | 0.6242 | 0.2639 |
| | 9 | | | | 1.0000 | 0.9999 | 0.9990 | 0.9940 | 0.9718 | 0.8926 | 0.6513 |
| | 10 | | | | | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 11 | 0 | 0.3138 | 0.0859 | 0.0422 | 0.0198 | 0.0036 | 0.0005 | 0.0000 | | | |
| | 1 | 0.6974 | 0.3221 | 0.1971 | 0.1130 | 0.0302 | 0.0059 | 0.0007 | 0.0000 | | |
| | 2 | 0.9104 | 0.6174 | 0.4552 | 0.3127 | 0.1189 | 0.0327 | 0.0059 | 0.0006 | 0.0000 | |
| | 3 | 0.9815 | 0.8389 | 0.7133 | 0.5696 | 0.2963 | 0.1133 | 0.0293 | 0.0043 | 0.0002 | |
| | 4 | 0.9972 | 0.9496 | 0.8854 | 0.7897 | 0.5328 | 0.2744 | 0.0994 | 0.0216 | 0.0020 | 0.0000 |
| | 5 | 0.9997 | 0.9883 | 0.9657 | 0.9218 | 0.7535 | 0.5000 | 0.2465 | 0.0782 | 0.0117 | 0.0003 |
| | 6 | 1.0000 | 0.9980 | 0.9924 | 0.9784 | 0.9006 | 0.7256 | 0.4672 | 0.2103 | 0.0504 | 0.0028 |
| | 7 | | 0.9998 | 0.9988 | 0.9957 | 0.9707 | 0.8867 | 0.7037 | 0.4304 | 0.1611 | 0.0185 |
| | 8 | | 1.0000 | 0.9999 | 0.9994 | 0.9941 | 0.9673 | 0.8811 | 0.6873 | 0.3826 | 0.0896 |
| | 9 | | | 1.0000 | 1.0000 | 0.9993 | 0.9941 | 0.9698 | 0.8870 | 0.6779 | 0.3026 |
| | 10 | | | | | 1.0000 | 0.9995 | 0.9964 | 0.9802 | 0.9141 | 0.6862 |
| | 11 | | | | | -, | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| | | | | | | * | | | | | |

Table A.1 Binomial Probability Table

Table A.1 (continued) Binomial Probability Sums $\sum_{x=0}^{r} b(x; n, p)$

| | | 707.0 | | | | <u>x=0</u> | | | | | |
|----|----|--------|--------|--------|--------|------------|--------|--------|--------|--------|-------|
| | | p | | | | | | | | | |
| n | r | 0.10 | 0.20 | 0.25 | 0.30 | 0.40 | 0.50 | 0.60 | 0.70 | 0.80 | 0.90 |
| 19 | 0 | 0.1351 | 0.0144 | 0.0042 | 0.0011 | 0.0001 | | | | 35334 | |
| | 1 | 0.4203 | 0.0829 | 0.0310 | 0.0104 | 0.0008 | 0.0000 | | | | |
| | 2 | 0.7054 | 0.2369 | 0.1113 | 0.0462 | 0.0055 | 0.0004 | 0.0000 | | | |
| | 3 | 0.8850 | 0.4551 | 0.2631 | 0.1332 | 0.0230 | 0.0022 | 0.0001 | | | |
| | 4 | 0.9648 | 0.6733 | 0.4654 | 0.2822 | 0.0696 | 0.0096 | 0.0006 | 0.0000 | | |
| | 5 | 0.9914 | 0.8369 | 0.6678 | 0.4739 | 0.1629 | 0.0318 | 0.0031 | 0.0001 | | |
| | 6 | 0.9983 | 0.9324 | 0.8251 | 0.6655 | 0.3081 | 0.0835 | 0.0116 | 0.0006 | | |
| | 7 | 0.9997 | 0.9767 | 0.9225 | 0.8180 | 0.4878 | 0.1796 | 0.0352 | 0.0028 | 0.0000 | |
| | 8 | 1.0000 | 0.9933 | 0.9713 | 0.9161 | 0.6675 | 0.3238 | 0.0885 | 0.0105 | 0.0003 | |
| | 9 | | 0.9984 | 0.9911 | 0.9674 | 0.8139 | 0.5000 | 0.1861 | 0.0326 | 0.0016 | |
| | 10 | | 0.9997 | 0.9977 | 0.9895 | 0.9115 | 0.6762 | 0.3325 | 0.0839 | 0.0067 | 0.000 |
| | 11 | | 1.0000 | 0.9995 | 0.9972 | 0.9648 | 0.8204 | 0.5122 | 0.1820 | 0.0233 | 0.000 |
| | 12 | | | 0.9999 | 0.9994 | 0.9884 | 0.9165 | 0.6919 | 0.3345 | 0.0676 | 0.001 |
| | 13 | | | 1.0000 | 0.9999 | 0.9969 | 0.9682 | 0.8371 | 0.5261 | 0.1631 | 0.008 |
| | 14 | | | | 1.0000 | 0.9994 | 0.9904 | 0.9304 | 0.7178 | 0.3267 | 0.035 |
| | 15 | | | | | 0.9999 | 0.9978 | 0.9770 | 0.8668 | 0.5449 | 0.115 |
| | 16 | | | | | 1.0000 | 0.9996 | 0.9945 | 0.9538 | 0.7631 | 0.294 |
| | 17 | | | | | | 1.0000 | 0.9992 | 0.9896 | 0.9171 | 0.579 |
| | 18 | | | | | | | 0.9999 | 0.9989 | 0.9856 | 0.864 |
| | 19 | | | | | | | 1.0000 | 1.0000 | 1.0000 | 1.000 |
| 20 | 0 | 0.1216 | 0.0115 | 0.0032 | 0.0008 | 0.0000 | | | | | |
| | 1 | 0.3917 | 0.0692 | 0.0243 | 0.0076 | 0.0005 | 0.0000 | | | | |
| | 2 | 0.6769 | 0.2061 | 0.0913 | 0.0355 | 0.0036 | 0.0002 | | | | |
| | 3 | 0.8670 | 0.4114 | 0.2252 | 0.1071 | 0.0160 | 0.0013 | 0.0000 | | | |
| | 4 | 0.9568 | 0.6296 | 0.4148 | 0.2375 | 0.0510 | 0.0059 | 0.0003 | | | |
| | 5 | 0.9887 | 0.8042 | 0.6172 | 0.4164 | 0.1256 | 0.0207 | 0.0016 | 0.0000 | | |
| | 6 | 0.9976 | 0.9133 | 0.7858 | 0.6080 | 0.2500 | 0.0577 | 0.0065 | 0.0003 | * | |
| | 7 | 0.9996 | 0.9679 | 0.8982 | 0.7723 | 0.4159 | 0.1316 | 0.0210 | 0.0013 | 0.0000 | |
| | 8 | 0.9999 | 0.9900 | 0.9591 | 0.8867 | 0.5956 | 0.2517 | 0.0565 | 0.0051 | 0.0001 | |
| | 9 | 1.0000 | 0.9974 | 0.9861 | 0.9520 | 0.7553 | 0.4119 | 0.1275 | 0.0171 | 0.0006 | |
| | 10 | 2,0000 | 0.9994 | 0.9961 | 0.9829 | 0.8725 | 0.5881 | 0.2447 | 0.0480 | 0.0026 | 0.000 |
| | 11 | | 0.9999 | 0.9991 | 0.9949 | 0.9435 | 0.7483 | 0.4044 | 0.1133 | 0.0100 | 0.000 |
| | 12 | | 1.0000 | 0.9998 | 0.9987 | 0.9790 | 0.8684 | 0.5841 | 0.2277 | 0.0321 | 0.000 |
| | 13 | | | 1.0000 | 0.9997 | 0.9935 | 0.9423 | 0.7500 | 0.3920 | 0.0867 | 0.002 |
| | 14 | | | | 1.0000 | 0.9984 | 0.9793 | 0.8744 | 0.5836 | 0.1958 | 0.011 |
| | 15 | | | | | 0.9997 | 0.9941 | 0.9490 | 0.7625 | 0.3704 | 0.043 |
| | 16 | | | | | 1.0000 | 0.9987 | 0.9840 | 0.8929 | 0.5886 | 0.133 |
| | 17 | | | | | | 0.9998 | 0.9964 | 0.9645 | 0.7939 | 0.323 |
| | 18 | | | | | | 1.0000 | 0.9995 | 0.9924 | 0.9308 | 0.608 |
| | 19 | | | | | | | 1.0000 | 0.9992 | 0.9885 | 0.878 |
| | 20 | | | | | | | | 1.0000 | 1.0000 | 1.000 |
| _ | | | | | | | | | | | |