

1 Assignment 4 Fourier Series; Approximation of Functions; Due to January 07, 2008

To construct the trigonometric polynomial of order M of the form

$$T_M(x) = \frac{A_0}{2} + \sum_{j=1}^M [A_j \cos(jx) + B_j \sin(jx)]$$

based on the N equally spaced values $x_k = -\pi + 2\pi k/N$, for $k = 1, 2, \dots, N$. The construction is possible provided that $2M + 1 \leq N$. You are given the program that constructs vectors A and B that contain the coefficients A_j and B_j , respectively, of the equation above of order M .

- Modify this program so that it will find the trigonometric polynomial of period $2P = d - c$ when data points are equally spaced over the interval $[c, d]$.
- Use your modified program to find $T_5(x)$ for

$$f(x) = -x^2 + 9 \text{ for } -3 \leq x < 3$$

using 60 equally spaced data points.

- Graph $T_5(x)$ and the data points on the same coordinate system.